

Objects, events, qualities

An introduction to formal ontological distinctions (in DOLCE)

Lecture 2 – Properties

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1 Outline

- Focus on non-temporary properties.
 - I will consider time and change in the next lecture.
- Philosophical theories of properties:
 - ▶ *Universalism*,
 - ▶ *Trope Theory*,
 - ▶ *Resemblance Nominalism*.
- How properties can be structured: philosophical, empirical, and cognitive perspectives on *hierarchies* and *spaces* of properties.
- How properties can be represented in FOL.
- Properties in DOLCE.

2 Properties

- Alternative names: *attributes*, *qualities*, *features*, *kinds*, *sorts*, *types*, *universals*.
- ▶ Do properties exist?
- ▶ Which properties there are?
- ▶ Which is the nature of properties?
- ▶ How properties can be represented?
- ★ Even though I will start the analysis of properties from philosophical theories, I do not want to rule out *concepts*.

3 Properties vs. individuals

- Are *properties* and *individuals* (*particulars*) two distinct ontological categories of entities?
 - ▶ Are individuals the substrates of their properties, or are they aggregates (*bundles*) of properties?
 - ▶ Are properties *repeatable* entities that apply to individuals, or are they abstractions reducible to *bundles of individuals*?
- Following a multiplicative approach I consider both *properties* and *individuals* in the domain.
 - ▶ I will analyze under which hypotheses properties can be reduced to (bundle of) individuals;
 - ▶ but I will **not** consider here theories that reduce individuals to bundles of properties (e.g. in Bertrand Russell).

4 Old problems

- *One over Many*

How can different individuals be of the same type?

How a and b can both have (share) the property P ?

- *Many over One*

How the same individual can have different properties?

How a can have both property P and property Q ?

- These two problems are intimately related to the analysis (in terms of *truth-makers*) of the sentence

- ▶ “ a has the property P ” or, shortly, “ a has P ”.

- Different theories of properties provide different answers/analyses.

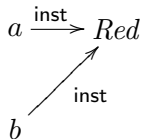
PHILOSOPHICAL THEORIES OF PROPERTIES

5 Universalism

- The *individual* a is an *instance* of the *universal* “being P ”.
- What makes it true that “ a has P ” is that the universal “being P ” is wholly present in a .
 - ▶ Categories: *individual* and *universal*.
Relation: *instantiation* $\text{inst} : \text{individual} \times \text{universal}$.
- Universals are *wholly* present in their instances, they are constituent parts of the instances.
- Universals are not (necessarily) *extensional*.
- Universals are *sparse & minimal* to capture the world’s distinctions.

6 Universalism: example

- Both the individuals a and b have the property “being red” (Red).



7 Universals vs. classes

- Classes are *partially* present in their instances and the instances are the constituents of classes (they depend on instances) while universals are *wholly* present in (but independent from) their instances.
- Classes are *extensional* while (in general) universals are *intensional*.
- Classes are *redundant* and *abundant* while universals are *sparse* and *minimal*: e.g. the union of two classes or the complement of a class are still classes, while the conjunction of two universals or the negation of a universal are not necessarily universals.
- **Natural classes.** Properties are *classes*, and the *natural classes* 'correspond' to universals.

8 Trope Theory

(1/2)

- The “*a*’s *P*-ness” *trope* (an individual) *inheres* in the individual *a* and it *exactly resembles* to *P*-ness tropes that inhere in different individuals (it *belongs* to the equivalence class of *P*-ness tropes).
- Tropes are *individual properties*: if $a \neq b$, then *a*’s *P*-ness (the way *a* is *P*) is different from *b*’s *P*-ness (the way *b* is *P*).
- What makes it true that an individual has a property is that it has a trope inhering in it that resembles other tropes (inhering in different individuals).
- Properties are then devoid of any ontological relevance, however they can be *associated* to equivalence classes of resembling tropes (i.e. abstractions on tropes by means of resemblance).

9 Trope Theory

(2/2)

- Categories: *individual*, *trope*, and *set*.

Relations: *inherence* $I : \text{trope} \times \text{individual}$;
 resemblance $\approx : \text{trope} \times \text{trope}$;
 membership $\in : \text{trope} \times \text{set}$.

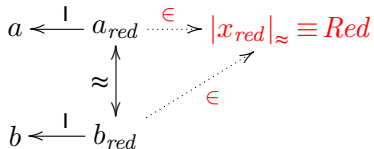
- Inherence standardly satisfies the *non migration principle*:

► $I(x, y) \wedge I(x, z) \rightarrow y = z$

i.e. tropes inhere only in one individual.

10 Trope Theory: example

- Both the individuals a and b have the property “being red”.



11 Trope Theory vs. Universalism

- Parallelism with theories of time and space:
 - *Substantivalism*: time (space) is a container-like manifold and what happens (exists) is located in it *contingently*.

Universalism: universals constitute an absolute and independent (from individuals) framework in which individuals are (contingently) located.

- *Relationism*: time (space) is derived from relationships between events (physical objects).

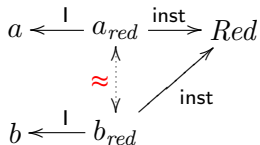
Trope Theory: properties are derived from (exact) resemblance between tropes (they can be associated to classes of exactly resembling tropes).

12 Universalism + Trope Theory

- Universalism and Trope Theory are not incompatible: it is possible to assume that universals are wholly present in tropes that inhere in individuals.
 - ▶ Categories: *individual*, *trope*, and *universal*.
Relations: *inherence* I : trope \times individual;
instantiation $inst$: trope \times universal.
- *Exact resemblance* can be defined: two tropes exactly resemble if and only if they are both instances of the same universal.

13 Universalism + Trope Theory: example

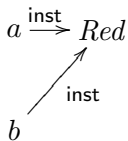
- Both the individuals a and b have the property “being red”.



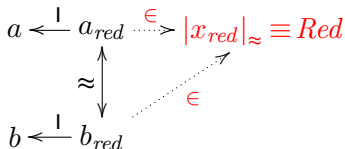
14 Main philosophical positions on properties

- Both the individuals a and b have the property “being red”.

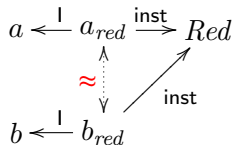
Universalism



Trope Theory



Universals+Tropes

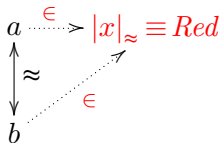


15 Resemblance Nominalism

- Individual a resembles to other particulars ('red' particulars).
- What makes it true that an individual has a property is that it resembles other individuals.
 - ▶ Categories: *individuals* and *class*.
Relations: *resemblance* \approx : individual \times individual
membership \in : individual \times class.
- Properties are devoid of any ontological relevance, however they can be *associated* to equivalence classes of resembling individuals, i.e. abstractions on individuals by means of resemblance.

16 Resemblance Nominalism: example

- Both the individuals a and b have the property “being red”.



17 Resemblance Nominalism: problems

- Resemblance Nominalism faces some difficult problems that, to be solved, require an ontological commitment:
 - ▶ *co-extensionality of properties*: how to distinguish extensionally coincident (they correspond to the same class) properties?
⇒ commitment to *possibilia*
(not work for *necessarily* co-extensional properties, e.g. 'being triangular', 'being trilateral' that Rodriguez-Pereyra identifies).
 - ▶ *change of properties*: the same object can persist through the change of properties
⇒ commitment to *temporal slices* of objects (*Perdurantism*)
(we will see in the next lecture).
- Possibilia are not necessary for Trope Theory while a sort of Perdurantism is necessary for the change of properties.

18 Resemblance Nominalism vs. Trope Theory (1/2)

- Relationism: the relations allowing to build time from events are different from the ones used to build space from physical objects.
- In general one can assume that properties can be abstracted from objects by using different resemblance relations: resemblance with respect to a specific aspect of the object.
- Resemblance Nominalism admits one resemblance relation, for this reason it has problems to differentiate co-extensional properties.
- Trope Theory admits one resemblance relation but on tropes that abstract one specific aspect from objects.

19 Resemblance Nominalism vs. Trope Theory (2/2)

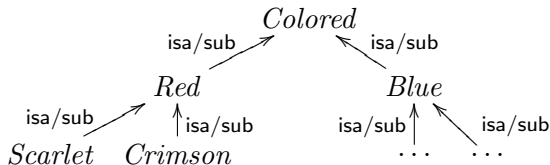
- A system $\langle D, \equiv^1, \dots, \equiv^n \rangle$
(where \equiv^i are resemblance relations on D)
 - ▶ is stronger than Resemblance Nominalism because of the presence of n different resemblance relations;
 - ▶ is weaker than trope theory because tropes cannot be reconstructed in it;
 - however tropicalists can adopt $\langle D, T^1, \dots, T^n, I, \equiv \rangle$
(where the T^j are disjoint sets of tropes, and I is the inherence relation) and define
$$x \equiv^j y \text{ iff } \exists t, s \in T^j (I(t, x) \wedge I(s, y) \wedge t \equiv s)$$

20 Abstraction process

- $\mathcal{S} = \langle D, \equiv \rangle$ is a generic structure with one *equivalence* relation.
- $\mathcal{S}^e = \langle D^e, =^e \rangle$ is the *abstraction* of \mathcal{S} , where
 - ▶ D^e is the set of (non-empty) equivalence classes of D ;
 - ▶ $=^e$ is the identity on D^e .
- Examples:
 - ▶ different (punctual) events can be temporally co-localized from $\mathcal{E} = \langle E, \equiv_E \rangle$, E set of *events*, \equiv_E *temporal coincidence* to $\mathcal{T} = \langle T, =^e \rangle$, T set of *times*.
 - ▶ different objects can have the same color from $\mathcal{O} = \langle O, \equiv_C \rangle$, O set of *objects*, \equiv_C *color resemblance* to $\mathcal{C} = \langle C, =^c \rangle$, C set of *color properties*.

TAXONOMIES OF PROPERTIES

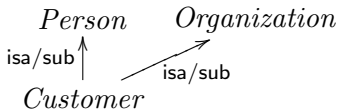
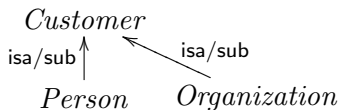
21 Isa/subsumption relation



- *isa/sub* is a very general hierarchical relation:
 - ▶ if x is 'Scarlet' *then* it is 'Red';
 - ▶ if x has property 'being Scarlet' it also has property 'being Red'.
- 'Scarlet' entails 'Red' because it is *impossible* for something to be scarlet without being red.
- In classical logic *isa/sub* is usually represented by *entailment*:
 - ▶ $Scarlet(x) \rightarrow Red(x)$ [semantically: $Scarlet^I \subseteq Red^I$]
(the *necessity* is not completely captured).

22 Digression: problems with isa

(1/3)

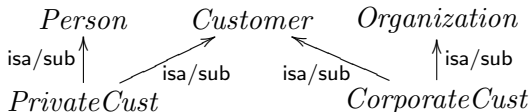


- Goal: only persons or organizations can be customers.
- But, neither all the persons are customers (first graph), nor all the customers are both persons and organizations (second graph).
- *Inheritance*:
 - ▶ in the first graph, the attributes of customers, e.g. 'customer code' are inherited by persons and organizations;
 - ▶ in the second graph, both the attributes of persons and organizations are inherited by customers, preventing the possibility to hide some private information about of persons and organizations.

23 *Digression: problems with isa*

(2/3)

- A possible solution requires additional properties:

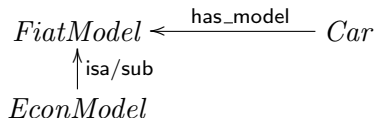


- Attributes of persons are inherited only by private customers (not by customers in general).
- *Subtle problem*: the same person can be a customer of different sellers, therefore the customer can have a number of different customer codes that is not fixed at the design time (it depends on the number of sellers).
- I will come back to this problem when I will talk of *roles*.

24 *Digression: problems with isa*

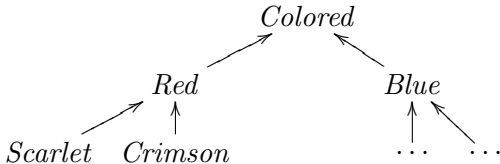
(3/3)

- Conceptual schema hold independently from specific individuals, therefore `has_model` needs to be introduced between properties.



- Different semantics for this link are possible:
 - ▶ $\text{has_model}(x, y) \rightarrow \text{Car}(x) \wedge \text{FiatModel}(y)$
 - ▶ $\text{Car}(x) \rightarrow \forall y(\text{has_model}(x, y) \rightarrow \text{FiatModel}(y))$
 - ▶ $\text{Car}(x) \rightarrow \exists y(\text{has_model}(x, y) \wedge \text{FiatModel}(y))$

25 Hierarchies of properties



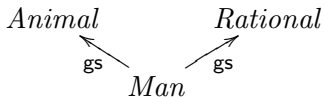
- *isa/sub* offers a purely *extensional* view on hierarchies, than does not necessarily fit well with Universalism and Trope theory.
- In particular, the *isa/sub* can be seen as too weak: it is a necessary but not a sufficient condition to be a *subproperty*.
- Which additional conditions need to satisfy the *subproperties* of a given property?

26 Genus-species

- *Genus-species* relations presuppose that more specific properties are conjunctions of independent properties, e.g. in

'Man is a rational animal'

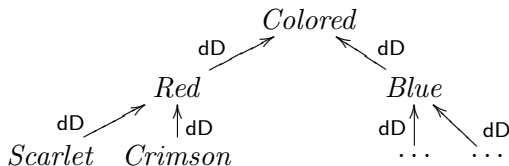
'rational' and 'animal' are independent (one does not entail the other one), and 'man' is the conjunction of them.



- The definition 'Scarlet is a red that is scarlet' does not work because 'scarlet' and 'red' are not independent ('scarlet' entails 'red').

27 Determinate-determinable: Johnson

(1/2)



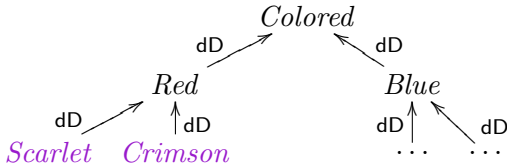
- Having a *determinate* property entails having a *determinable* property (e.g. *Scarlet* implies *Colored*) .
- Having a *determinable* property entails having *one and only one* of its full *determinates* (no instances of both *Scarlet* and *Crimson*).

28 Determinate-determinable: Johnson

(2/2)

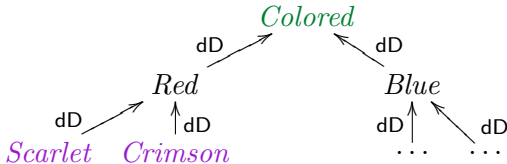
- 'Color' *generates* 'scarlet', 'crimson', etc. To understand 'color' one needs the notions of 'scarlet', 'crimson', etc. ('animal' does not require 'man', 'dog', etc.) [*adjectives* vs. *substantives*].
- To grasp 'color' one needs to grasp how different shades of color are different from one another while still being shades of color.
- The grasping of *determinables* involves the grasping of certain relations of *similarity* or *intensification* used to generate their determinates.
- Determinates under the same determinable are different but comparable, e.g., under the determinable 'color', 'red' is more similar to 'orange' than to 'yellow'.

29 Full determinates



- *Full determinates* admit no more than a difference between any two instances with regard to the relations of intensification by which they are generated (leaves in a hierarchy).
- E.g., the instances of a specific shade of color (e.g., let us suppose, *Scarlet*) are all the same with respect to color.
- Shades are colors, but not all colors are shades, since some colors consist of collections of shades ordered by some relation that is included in our grasp of the color (e.g. *Red* and *Blue*).

30 General determinables

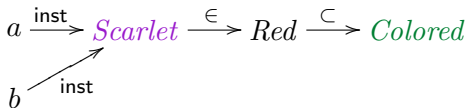


- Incompatibility of full determinates: as already stated, having a *determinable* entails having *one and only one* of its full *determinates*.
- Comparability: instances of full determinates under a general determinable are (at least qualitatively) comparable. (The color of an object is not comparable with the shape of another one).
- *General determinables* are maximal with respect to comparability of their determinates.

31 Determinate-determinable: Universalism

- Determinables are experimentally derivative from full determinates, they are specified bottom-up by enumeration of full determinates.
- To assert that a particular is red is to assert that it has some property, a property that is a member of a certain class of properties: the class of all full determinate shades of red.
- All genuine *universals* are full determinates because instances of an universal need to be *identical* in a certain respect.
- But what constitute the *unity* of this class (of properties)?
 - ▶ Church: an ordering/resemblance relation between universals.
 - ▶ Armstrong: partial identity (based on parthood) of universals, on the basis of which a sort of resemblance can be defined.
- Johnson: determinables rely on an intensification/ordering relation.

32 Predication of determinables: Universalism

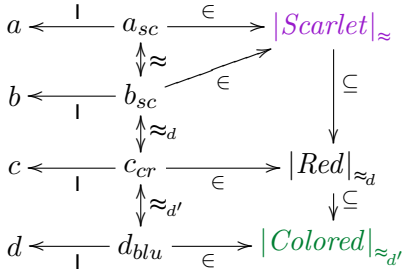


- Full determinates correspond to universals.
- Determinables correspond to *sets* of full determinates (are they *conceptual* constructions?).
- *General* determinables collect universals that satisfy unity conditions based on:
 - ▶ resemblance/comparability relation (with degrees) between universals [Church];
 - ▶ partial identity (and parthood) between universals on the basis of which a comparability relation can be defined [Armstrong].

33 Determinates-determinables: Trope theory

- First of all one needs to understand if tropes are maximally specified or not: do the 'the red of the rose r ' and 'the color of r ' exist?
- Accepting only maximally specified tropes
 - ▶ full determinates correspond to classes of *exactly* resembling tropes;
 - ▶ determinables correspond to classes of *inexactly* resembling tropes (e.g. 'the scarlet of r_1 ' and 'the crimson of r_2 '), therefore inexact resemblance (*with degree*) is needed.
- In principle the inexact resemblance does not collect the whole class of tropes, but it stops at the level of the *general determinables* that therefore correspond to *maximal* classes of inexactly resembling tropes.
- This last aspect is quite critical.

34 Predication of determinables: Trope theory



- *Full determinates* correspond to classes of *exactly* resembling tropes.
- *Determinables* correspond to classes of *inexactly* resembling tropes.
- *General determinables* corresponds to *maximal* classes of inexactly resembling tropes.

SPACES OF PROPERTIES

35 Ontological similarity and comparability

- Universalism and Trope Theory both consider that two entities are *similar* when and because they 'share a fully determinate property':
 - ▶ they share a universal (*universalism*);
 - ▶ they have exactly resemblant tropes (*trope theory*).
- In this case, *similarity* is *objective*, *mind* and *language* independent, it is exclusively based on the *ontological nature of entities* providing the *finest* possible analysis.
- Similarity with degree and partial identity allow to 'abstract' from the objective nature of full determinates.
- Entities sharing a *general determinable* are not *exactly similar* but at least *comparable*.

36 Towards an empirical/epistemological level

- “[J]udgments of similarity (...) are central for a large number of cognitive processes. (...) such judgments reveal the dimensions of our perceptions and their structures.” [Gärdenfors, 2000]
- In this case, *similarity* is empirically built on experiments and it is *relative*: it may depend on species, cultures, etc.
- In *science*, the analysis always is conducted at an empirical (or theoretical) level and it depends on the available information, the measurement instruments/methods, the specific theory considered, etc.
- Not only it is possible to abstract from full determinates, but it is possible to consider different full determinates (they are no more *objective*) that can be structured in different ways.
- If we have time, we will consider measurement in the next lecture.

37 Spaces of properties

(1/2)

- These more epistemological properties (**concepts?**) can be structured in *spaces of properties* that reflect a particular empirical or epistemological point of view and not a purely ontological one.
- The determinates of a general determinable can be arranged in different *spaces* with:
 - ▶ different full determinates (different resemblance/identity);
 - ▶ different determinables (different granularities/degrees of resemblance);
 - ▶ different structures (different comparability).

38 Spaces of properties

(2/2)

- Resemblance with *degree* or partial identity introduce a (partial) order among properties.
 - ▶ Spaces can have a topological or geometrical structure (more expressive relations are needed).
- To a general determinate can be associated more spaces that depend on culture, instruments of investigation, etc.
- In this view, spaces exist *in time*: they are created, adopted, and destroyed by (communities of) intentional agents.

39 Conceptual spaces: Peter Gärdenfors

(1/2)

- Conceptual spaces are collections of related *domains* each of which is a collection of (integral and separable) *dimensions*, e.g. temperature, weight, pitch, and brightness.
- Dimensions correspond to “the different ways stimuli are judged to be similar or different” .
- A point in a dimension represents a specific property (e.g. a temperature) and the association of two objects to the same point represents the experimental fact that the two objects are completely *similar* with respect to that dimension (e.g. temperature).
- Points can be ordered (e.g. temperatures can be “low” or “high”) therefore each dimension is endowed with a (pseudo) metric that represents the level of similarity between stimuli.

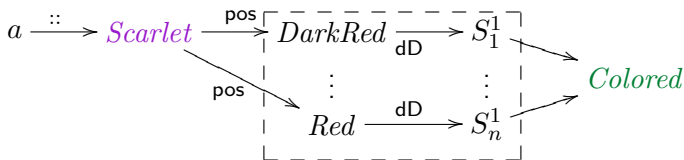
40 Conceptual spaces: Peter Gärdenfors

(2/2)

- A set of dimensions is *integral* if an object is located in one dimension, necessarily it is located in all the other dimensions.
 - ▶ E.g., {*hue*, *brightness*} is integral: if an object has a particular hue it necessarily has also a particular brightness and vice versa.
- *Domains* are maximal sets of integral dimensions.
 - ▶ E.g. {*hue*, *chromaticness*, *brightness*} form a domain (color) because it is integral but *hue*, *chromaticness* and *brightness* are separable from any dimension that does not belong to this set.
- A property corresponds to a *region* in a domain.
- *Conceptual spaces* are collections of one or more domains, and their regions represent *concepts* (points in conceptual spaces correspond to the more specific concepts).

41 Spaces with the same full determinates

- Full determinates are 'objective' but they can be *contextually* organized in different spaces.

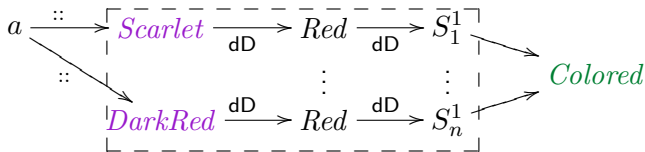


where $::$ stands for *inst* in Universalism or for a composition of \mid and \in in Trope theory, and pos is a general relation to represent the fact that *Scarlet* has a specific position in a space.

- To the same general determinable, different spaces with different (non full) determinates can be associated, e.g. *DarkRed* is not considered in space S_n^1 .

42 Spaces with different full determinates

- Both full determinates and structures of spaces are *contextual*.



- If we assume that for each general determinable there is a space S^* with maximal granularity (as defined by, say, a *refinement relation*), then the atomic regions of S^* can be taken to be the the “objective” full determinates.
- Again, to individuate all the spaces relative to the same domain or dimension (general determinable) an additional relation is necessary.

*REPRESENTING PROPERTIES AND SPACES
IN FIRST ORDER LOGIC*

43 Properties as predicates

(1/2)

- $\text{Red}(x) \wedge \text{Orange}(y) \wedge \text{Blue}(z) \wedge \text{Sim}_C(x, y, z)$
- (Some) Universalists
 - ▶ refuse extensionality (universals are not just sets of entities);
 - ▶ Boolean (logical) combination of universals are not universals.
- (Some) Conceptualists
 - ▶ assume that concepts are created, they can disappear and depend on societies or groups of agents that use them: *properties of properties*.
- In FOL, one can:
 - ▶ *reify* properties into the domain of quantification, and
 - ▶ introduce a non extensional relation of *instantiation*.

44 Properties as predicates

(2/2)

■ (Some) Tropicalists

have less problems to accept extensionality and Boolean closure, because they just *associate* (and do not identify) properties to sets of tropes, however they require a deeper analysis in terms of *inherence* and tropes:

- ▶ $\text{Red}(x) \triangleq \exists r_t (I(r_t, x) \wedge \text{Red}_T(r_t))$
- ▶ $\text{Sim}_C(x, y, z) \triangleq \exists c_t, c'_t, c''_t (\text{Color}_T(c_t) \wedge \text{Color}_T(c'_t) \wedge \text{Color}_T(c''_t) \wedge I(c_t, y) \wedge I(c'_t, x) \wedge I(c''_t, z) \wedge \text{Sim}_T(c_t, c'_t, c''_t))$
- ▶ $\text{Crimson}_T(c_t) \wedge \text{Crimson}_T(c'_t) \rightarrow c_t \approx c'_t$ (for full determinates)

where

- ▶ P_T indicates a class of tropes, and
- ▶ Sim_T is a similarity relation defined on tropes.

45 Properties as attributes

- $\text{Color}(x, \text{red}) \wedge \text{Color}(y, \text{orange}) \wedge \text{Color}(z, \text{blue}) \wedge \text{Sim}_P(\text{red}, \text{orange}, \text{blue})$
 - ▶ $\text{Red}(x) \triangleq \text{Color}(x, \text{red})$
 - ▶ $\text{Sim}_C(x, y, z) \triangleq \exists c_p, c'_p, c''_p (\text{Color}(x, c_p) \wedge \text{Color}(y, c'_p) \wedge \text{Color}(z, c''_p) \wedge \text{Sim}_P(c_p, c'_p, c''_p))$
- In UML, function $\text{color}: \text{Apple} \rightarrow \text{Color}$



where *Color* is a *datatype*, i.e. a class of *values* (not *objects*).

- To impose the functional requirement
 - ▶ $\text{Color}(x, y) \wedge \text{Color}(x, z) \rightarrow y = z$

46 Attribute functions

(1/2)

- Each *function/datatype* corresponds to a general determinable.
- Each *value* corresponds to a full determinate.
- The functional view admit only full determinates are in the domain of quantificationis and is, in general, not extensional:
 $\text{Color}(x, \text{crimson}) \leftrightarrow \text{Length}(x, 1\text{m})$ does not entail $\text{crimson} = 1\text{m}$.
- Predication on values allows to express dependences, structures, time stamp, etc.
- Bunge-Weber-Wand provided an universalistic interpretation to attributes, however a trope-theoretical interpretation is possible (where classes of tropes that correspond to attribute values are needed):
 - ▶ $\text{Color}(x, \text{crimson}) \leftrightarrow \exists c_t (I(c_t, x) \wedge \text{Crimson}_T(c_t))$

47 Attribute functions

(2/2)

- To represent non-full determinables, one needs:
 - ▶ to include non-full determinates in the 'values' discarding the functionality constraints:
$$\text{Color}(x, \text{crimson}) \wedge \text{Color}(x, \text{red}) \wedge \text{crimson} \neq \text{red},$$
$$\text{Color}(x, \text{crimson}) \rightarrow \text{Color}(x, \text{red});$$
 - ▶ or to treat non-full determinables as predicates defined in terms of disjunctions of full determinates, e.g.
$$\text{Red}(x) \triangleq \text{Color}(x, \text{crimson}) \vee \dots \vee \text{Color}(x, \text{scarlet}).$$

48 *Digression*: full determinates vs. values

- What is the ontological nature of values?
 1. Can the same value be used for different attributes? For example, can '1m' be used for *height* and *length*?
 2. Do '1m' and '100cm' refer to two different values?
- Full determinates are specific properties, therefore 'being 1m high' and 'being 1m long' are just two different properties.
- The same full determinate can be 'measured' in different ways: 'being 1m high' and 'being 100cm high' refer to the same property but to different *measurement systems*.
- 'm' and 'cm' can refer to different granularities or measurement's precisions.

49 Reification of properties and instantiation

- $\text{inst}(x, \text{red}) \wedge \text{Color}(\text{red}) \wedge \text{inst}(y, \text{orange}) \wedge \text{Color}(\text{orange}) \wedge \text{inst}(z, \text{blue}) \wedge \text{Color}(\text{blue}) \wedge \text{Sim}_P(\text{red}, \text{orange}, \text{blue})$
 - ▶ $\text{Color}(x, y) \triangleq \text{inst}(x, y) \wedge \text{Color}(y)$
 - ▶ $\text{Sim}_C(x, y, z) \triangleq \exists c_p, c'_p, c''_p (\text{Color}(x, c_p) \wedge \text{Color}(y, c'_p) \wedge \text{Color}(z, c''_p) \wedge \text{Sim}_P(c_p, c'_p, c''_p))$
- Compatible both with Universalism and Trope Theory.
- Similar to attributes but:
 - ▶ general determinables correspond to unary predicates;
 - ▶ full determinates and determinables are both in the domain;
 - ▶ full-determinate can be distinguished from determinates:
 $\text{Color}(\text{red}) \wedge \text{Color}(\text{crimson}) \wedge \forall x (\text{inst}(x, \text{crimson}) \rightarrow \text{inst}(x, \text{red}));$
 - the *instantiation* relation (inst) needs to be characterized.

*PROPERTIES AND SPACES IN
DOLCE AND DOLCE-CORE*

50 Properties and spaces in DOLCE

- The intuition is very close to the last framework we considered:
 - ▶ Both determinables and full-determinates are in the domain of quantification;
 - ▶ A sort of *instantiation* relation, called *quale* (ql) in DOLCE, is considered.
- However DOLCE introduces some novelties.

51 Properties as regions

- General determinables do not correspond to predicates but, as in the case of determinables and full-determinates, to *spatial regions*.
- The determinable-determinate relation is represented by means of a *classical extensional mereology* based on *parthood simpliciter* (P):
 - ▶ full determinates correspond to *atomic regions* (called *qualia*)
$$\text{At}(x) \triangleq \forall y (\text{P}(y, x) \rightarrow y = x);$$
 - ▶ general determinables correspond to regions called *spaces* that include their determinates, e.g. $\text{P}(\text{crimson}, \text{red}) \wedge \text{P}(\text{red}, \text{color})$;
 - ▶ structural constraints can be introduced among regions.
- DOLCE admits only one space for each general determinable.
- Spaces in DOLCE are similar to conceptual spaces of Gärdenfors, but properties do not need to correspond to self-connected regions.

52 Individual qualities

(1/3)

- Ontologically, the dimension of classification of entities or the aspect along they are compared seems a quite obscure notion.
- To represent this 'aspect' or 'dimension' of classification, DOLCE introduces the notion of *individual quality*.
- We will analyze the differences between individual qualities and tropes. For the moment, just note that:
 - ▶ like tropes, they inhere in a specific object: the weight of John is different from the weight of Sam;
 - ▶ differently from tropes, they persist through change: the weight of John (the same individual quality) can be associated to different full determinates (qualia) at different times.
- The inherence relation is called *quality* (qt) in DOLCE.

53 Individual qualities

(2/3)

- Dimensions/aspect can be identified by a *comparability* relation on individual qualities. DOLCE follows an alternative (but equivalent) solution that assumes n disjoint predicates QT_i (called *quality kinds*), one for each dimension/aspect (e.g. Q_{color} , Q_{weight}).
- Spaces can be characterized on the basis of the Q_i predicates as regions x that are mereologically maximal regions that satisfy the following property:

$$\forall q, q', r, r' (P(r, x) \wedge P(r', x) \wedge ql(r, q) \wedge ql(r', q') \wedge Q_i(q) \rightarrow Q_i(q'))$$

i.e. they collect all the region that classify comparable individual qualities (individual qualities of the same kind).

54 Individual qualities

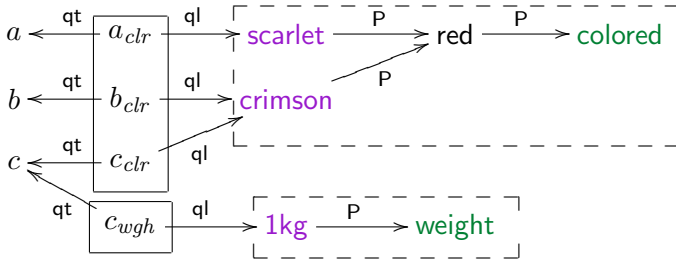
(3/3)

- Individual qualities allow also for a more 'direct' semantics of some NL expressions.
 - This rose is red.
 - Red is a color.
 - This rose has a color.
 - The color of this rose turned to brown in one week.
 - Red is opposite to green and close to brown.
 - The patients temperature is increasing.
 - The doctor measured the patient's temperature.

55 *Digression:* International System of Units

- A similar approach is adopted by the SI, where:
 - ▶ quantities in the *particular* sense correspond to individual qualities;
 - ▶ quantities in the *general* sense correspond to general determinables.

56 General schema in DOLCE



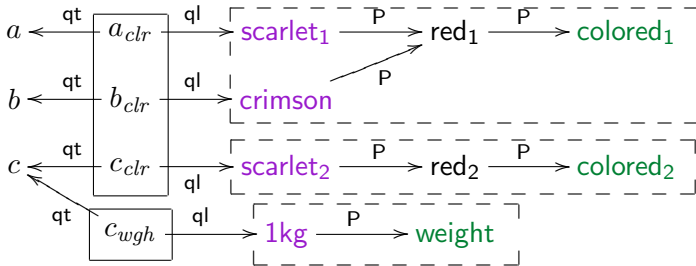
$$\text{Color}(x, \text{red}) \triangleq \exists q, y (\text{qt}(q, x) \wedge \text{ql}(y, q) \wedge \text{P}(y, \text{red}) \wedge \text{P}(\text{red}, \text{colored}))$$

- a_{clr} , the color individual quality that inheres in a , represents the dimension/aspect of a that we are classifying.

57 Properties and spaces in DOLCE-CORE

- More standard terminology:
 - ▶ *inherence* (I) instead of *quale* (ql);
 - ▶ *location* (L) instead of *quality* (qt).
- DOLCE-CORE modifies DOLCE to associate different spaces to the same dimension/aspect of classification (i.e. different spaces can be associated to the same quality kind Q_i): *cognitive/empirical move*.
- Different spaces do not overlap (no common regions) even though they are relative to the same dimension.
 - ▶ The previous maximality condition does not work.
 - ▶ A finite set of disjoint primitive predicates S_1^i, \dots, S_n^i that correspond to different spaces is associated to each quality kind Q_i :
$$S_j^i(x) \wedge P(r, x) \wedge L(r, q) \rightarrow Q_i(q).$$

58 General schema in DOLCE-CORE



- To compare regions inside different spaces associated to the same quality kind new relations are necessary.
- A *refinement relation* between spaces allows to introduce a notion of *granularity* and to select the most refined spaces (if unique, the most refined space is an empirical surrogate of objectivity).

59 Properties in DOLCE and DOLCE-CORE

- This is not the whole story:
 - ▶ time and change need to be taken into account;
 - ▶ properties that are not organized in spaces need to be taken into account.
- These are the topic of the next lecture!